



Formation Adaptation in Obstacle-Cluttered Environments via MPC-Based Trajectory Planning

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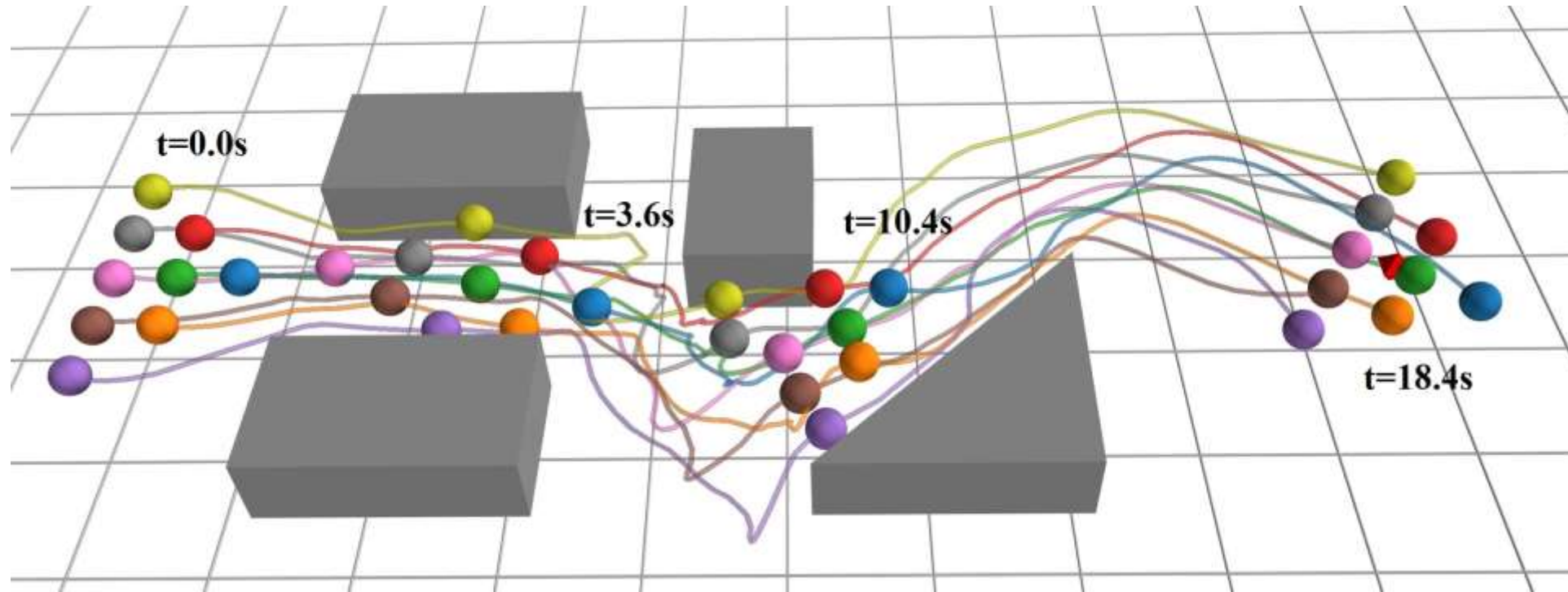
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Content

- **Motivation**
- **Proposed Method**
- **Results**
- **Conclusions**

- ◆ Formation is a typical collective behavior in multi-agent system, which has applications in inspection, surveillance, transportation.
- ◆ Current formation methods includes: virtual structure, consensus-based methods and affine formation.
- ◆ Though these feedback control methods have high robustness and low computation cost, yet they neglect the **obstacle-cluttered environment**.

Motivation



More specifically, the agents need to **adapt** their formation structure to safely pass some narrow passages or corners like the above figure.

Current works:

Recent works [1,2] propose an interesting idea of adopting trajectory planning to achieve formation and meanwhile avoid obstacle collisions. Specifically, they reformulate the planning as numerical optimization problems and enforce soft or hard constraints to avoid obstacles and inter-agent collision.

[1] Javier A, Stuart B, Daniela R. Multi-agent formation control and object transport in dynamic environments via constrained optimization. *The International Journal of Robotics Research*, 2017, 36:1000-1021.

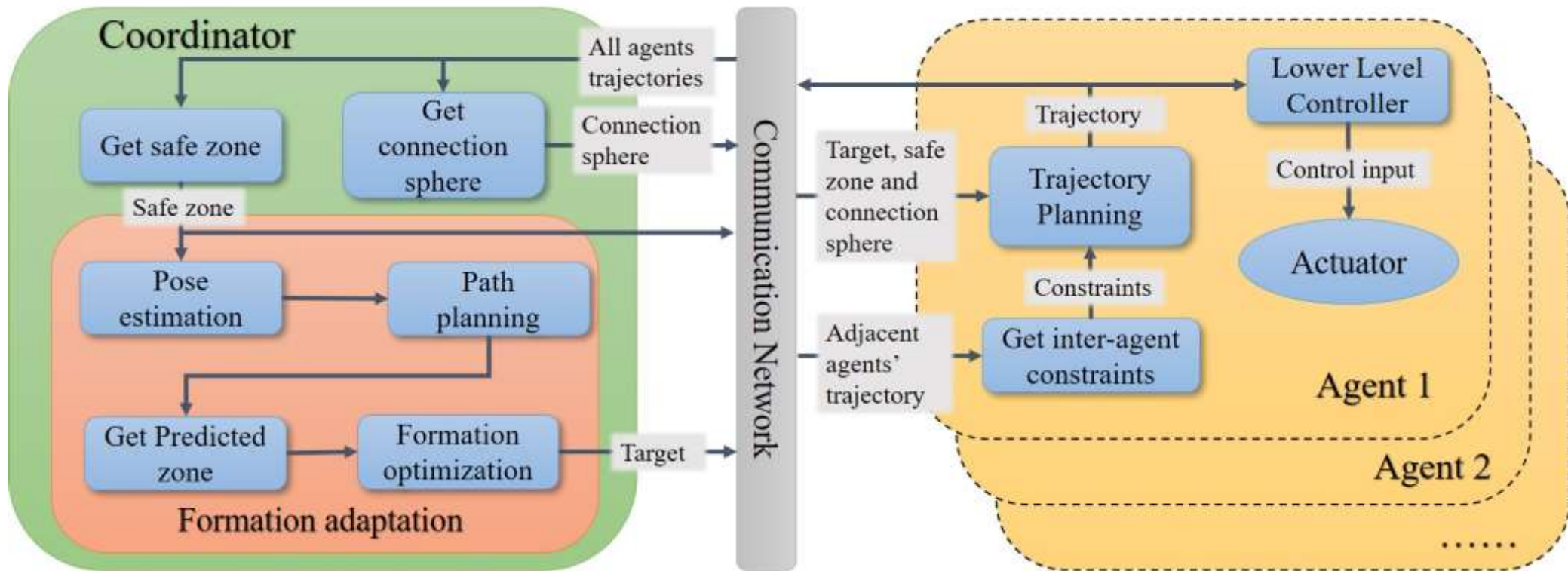
[2] Quan L, Yin L, Zhang T, et al. Robust and efficient trajectory planning for formation flight in dense environments. *IEEE Transactions on Robotics*, 2023, 1-20.

The main difficulties of current works:

- ◆ The induced constrained optimization is not ensured to be feasible in the sense that the **safety** of the underlying agents in terms of agent-obstacle and inter-agent collision avoidance **is not theoretically guaranteed**.
- ◆ Inter-agent communication in the formation, e.g., the **line-of-sight collision** between agents, is not adequately concerned.

Therefore, we propose a novel formation adaption method via MPC (model predictive control)-based trajectory planning, with both collision avoidance and connectivity maintenance ensured. Formation adaptation is encoded to achieve adaptive deformation according to the obstacle distribution.

Proposed Method



The scheme of the proposed method.

Proposed Method



Safe zone:

$$a_m^{\text{zone}T} p_k^i \geq b_m^{\text{zone}}, m \in \mathcal{M}$$

where

$$\begin{aligned} & a_m^{\text{zone}}, b_m^{\text{zone}}, \delta, \\ \text{s.t. } & a_m^{\text{zone}T} p \geq \delta + b_m^{\text{zone}}, p \in \mathcal{P}^{\text{free}} \\ & a_m^{\text{zone}T} p \leq b_m^{\text{zone}}, p \in \mathcal{P}_m^O, \\ & \|a_m^{\text{zone}}\|_2 = 1, \end{aligned}$$

Inter-agent constraints:

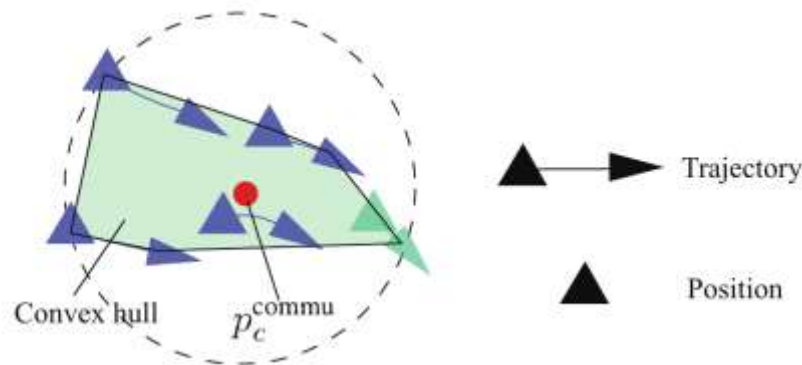
$$a_k^{ijT} p_k^i \geq b_k^{ij}, \forall j \neq i, \forall k \in \mathcal{K}$$

where

$$a_k^{ij} = \frac{\bar{p}_k^i - \bar{p}_k^j}{\|\bar{p}_k^i - \bar{p}_k^j\|_2}, b_k^{ij} = a_k^{ijT} \frac{\bar{p}_k^i + \bar{p}_k^j}{2} + \frac{r'_{\min}}{2}$$

$$r'_{\min} = \sqrt{4r_a^2 + h^2 v_{\max}^2}$$

Communication sphere:



$$\|\bar{p}_k^i - p_c^{\text{commu}}\|_2 \leq d_c$$

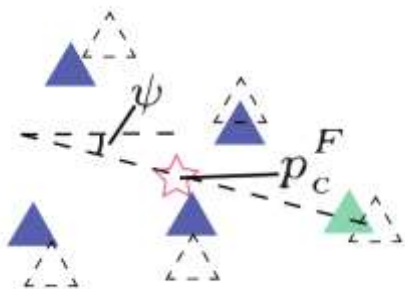
where

$$\begin{aligned} & d, p_c^{\text{commu}} \\ \text{s.t. } & \|p_c^{\text{commu}} - \bar{p}_k^i\|_2 \leq d \end{aligned}$$

Proposed Method



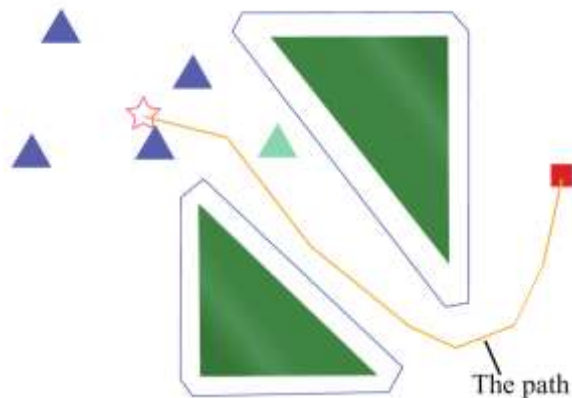
Pose estimation:



$$\min_{\psi, p_c^F} \sum_{i=1}^N \|R^i(\psi)r^i + p_c^F - p_K^i\|_2^2$$
$$\text{s.t. } |\psi(t-h) - \psi| \leq \delta\psi_{\max}$$

where $\mathcal{R}(\psi) = \mathcal{R}(\psi(t-h)) + \frac{\partial \mathcal{R}(\theta)}{\partial \theta} \Big|_{\theta=\psi(t-h)} (\psi - \psi(t-h))$

Path planning:

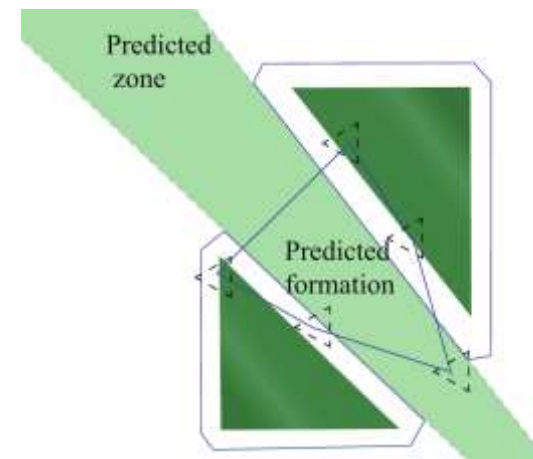
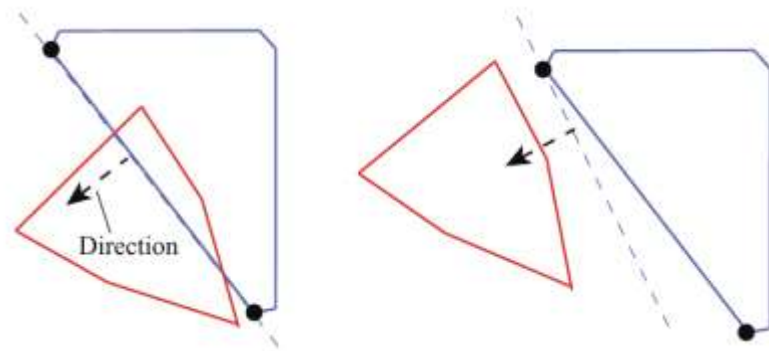


Inflate obstacles and, then, plan a path via RRT* based method.

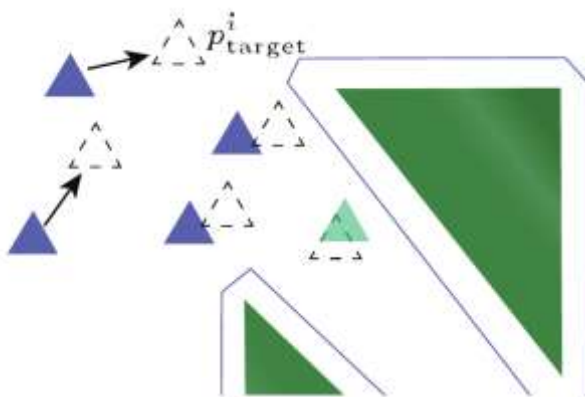
Proposed Method



Predicted zone derivation:



Formation optimization:



$$\begin{aligned}
 & \min_{\bar{\psi}, p_{\text{target}}^i, w} \quad \|p_{\text{target}}^0 - p_{\text{tractive}}\|_2^2 + \alpha_w w^2 \\
 & \quad + \sum_{i=1}^N \|\mathcal{R}(\bar{\psi})r^i + p_{\text{target}}^0 - p_{\text{target}}^i\|_2^2 \\
 & \text{s.t.} \quad a_m^{\text{zoneT}} p_{\text{target}}^i + b_m^{\text{zone}} + w \geq 0, m \in \mathcal{M} \\
 & \quad a_m^{\text{preT}} p_{\text{target}}^i + b_m^{\text{pre}} + w \geq 0, m \in \mathcal{M} \\
 & \quad w \geq 0,
 \end{aligned}$$

Proposed Method



Finally, the following optimization problem is carried out in each agent

$$\begin{aligned} & \min_{u_{k-1}^i, x_k^i, k \in \mathcal{K}} C^i && \text{Objective function} \\ \text{s.t. } & x_k^i = \mathbf{A}x_{k-1}^i + \mathbf{B}u_{k-1}^i, k \in \mathcal{K}, && \left. \begin{array}{l} \text{Dynamic constraints} \\ \text{Inter-agent collision constraints} \\ \text{Obstacle collision constraints} \\ \text{Connectivity constraints} \\ \text{Terminal constraints} \end{array} \right\} \\ & \|\Theta_a u_{k-1}^i\|_2 \leq a_{\max}, k \in \mathcal{K}, \\ & \|\Theta_v v_k^i\|_2 \leq v_{\max}, k \in \mathcal{K}, \\ & a_k^{ijT} p_k^i \geq b_k^{ij}, \forall j \neq i, k \in \mathcal{K}, \\ & a_m^{\text{zone}T} p_k^i \geq b_m^{\text{zone}}, m \in \mathcal{M}, k \in \mathcal{K}, \\ & \|\bar{p}_k^i - p_c^{\text{commu}}\|_2 \leq d_c, k \in \mathcal{K}, \\ & v_K^i = \mathbf{0}_d. \end{aligned}$$

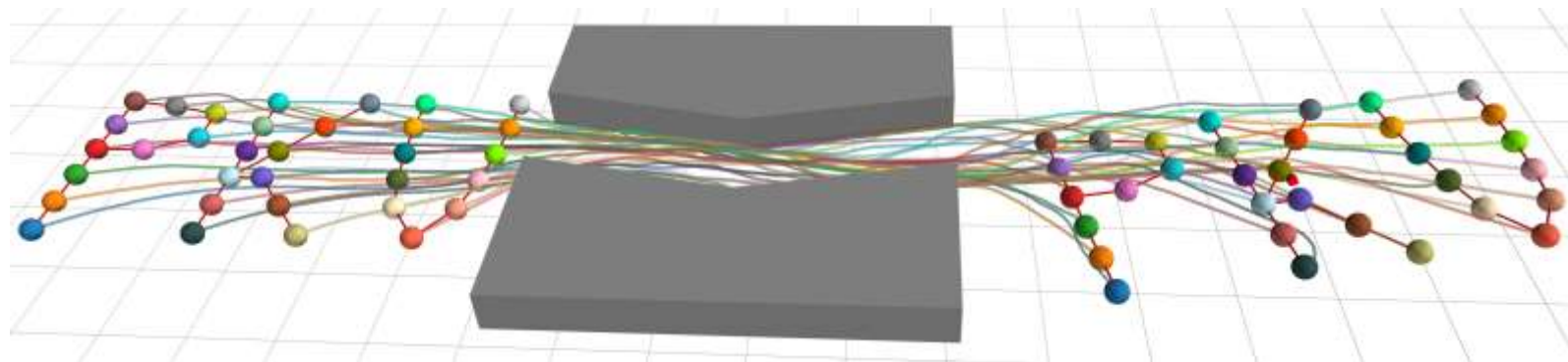
The objective function is determined as follows:

$$\frac{1}{2} Q_K \|p_K^i - p_{\text{target}}^i\|_2^2 + \frac{1}{2} \sum_{k=1}^{K-1} Q_k \|p_{k+1}^i - p_k^i\|_2^2$$

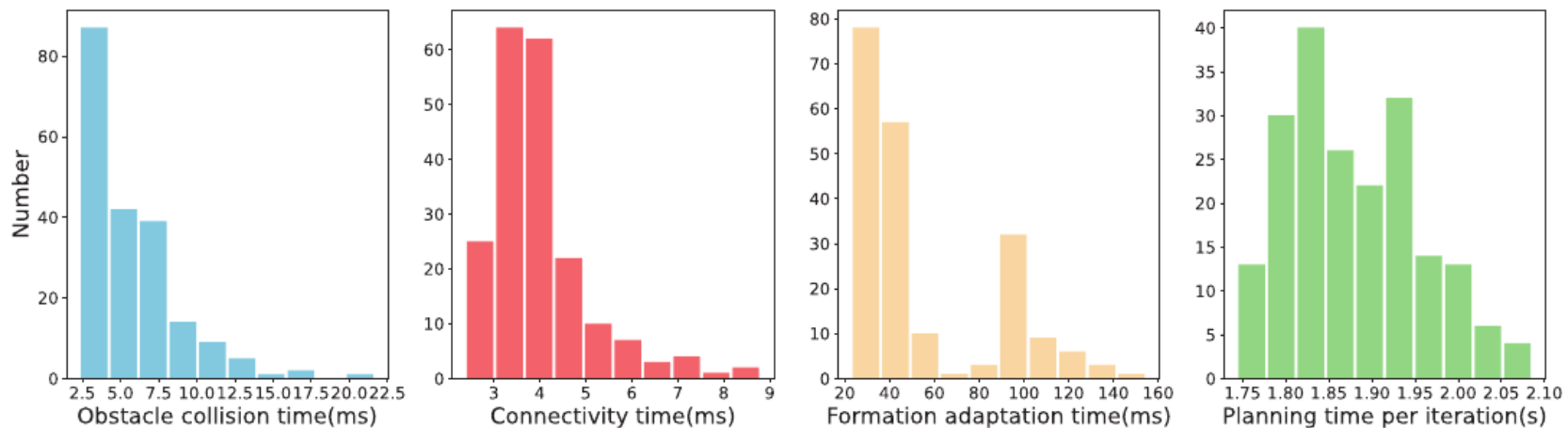
Property:

By adopting the proposed method, if the agents are initially connected and collision-free, then they can maintain connectivity and be collision-free thereafter.

Simulation 1:



The trajectories of the underlying agents.

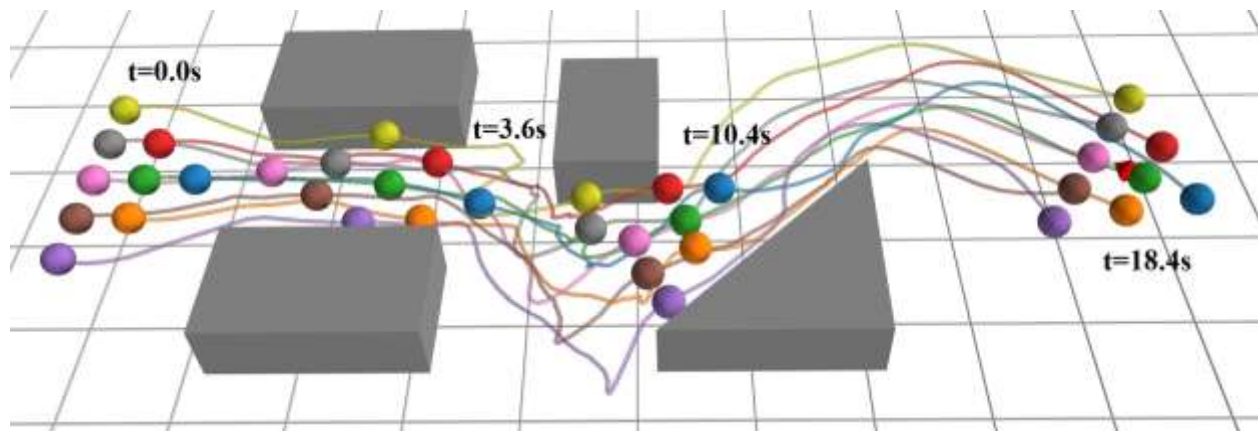


From left to right is the times of runtime w.r.t. different parts in a replanning.

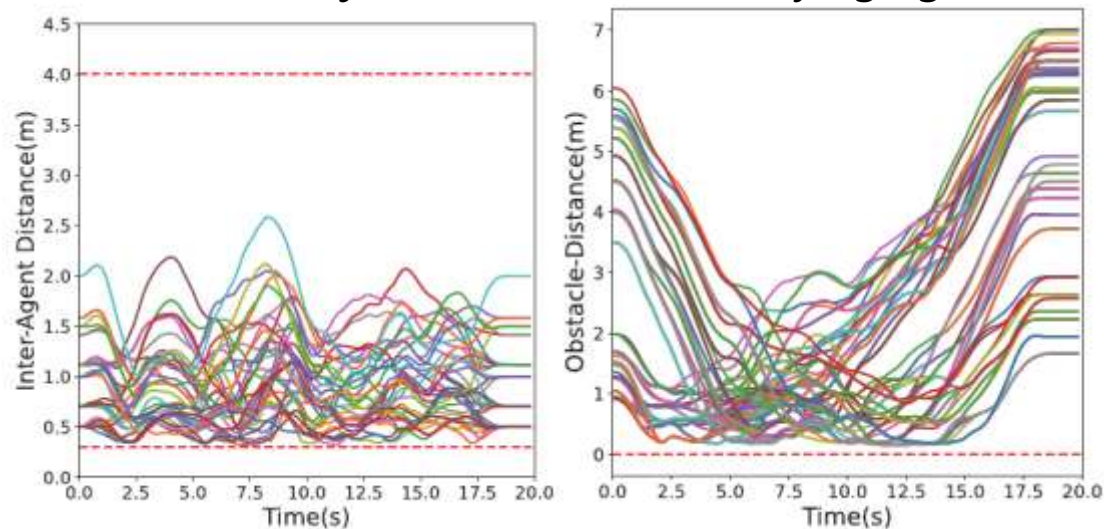
Results



Simulation 2:



The trajectories of the underlying agents.

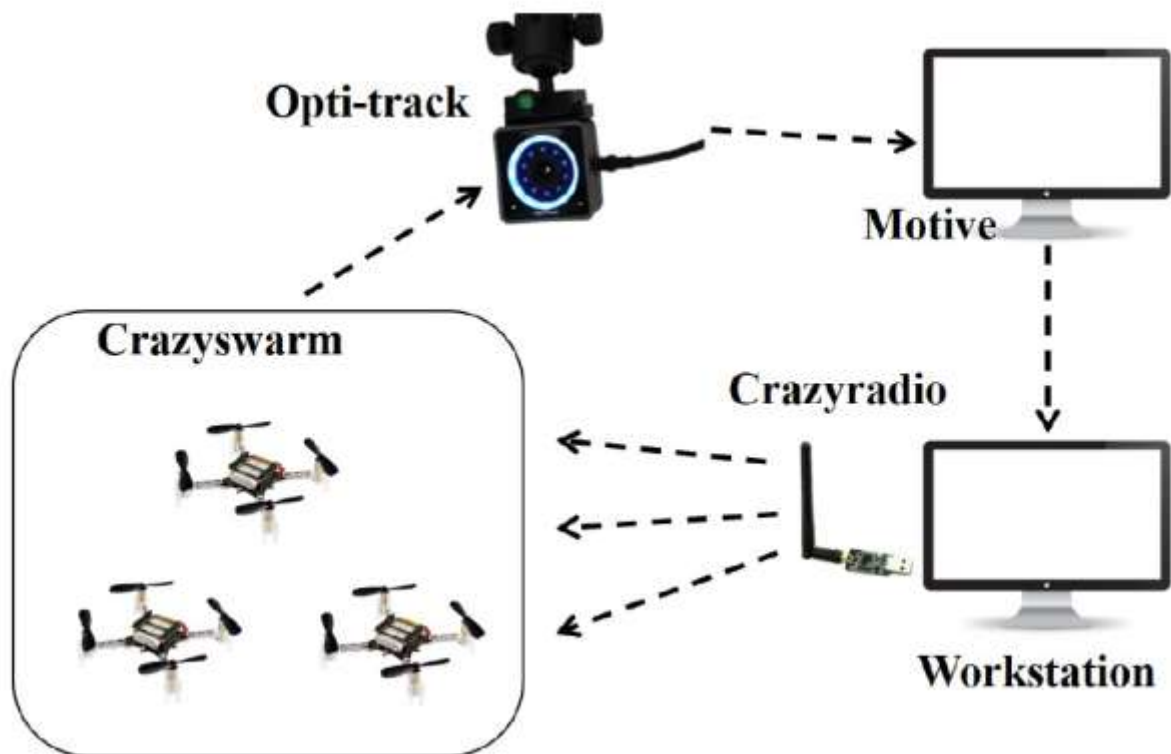


Left: the distance between each pair of agents. Right: the distance between LOS of each pair of agents and obstacles.

Results



Experiment platform:

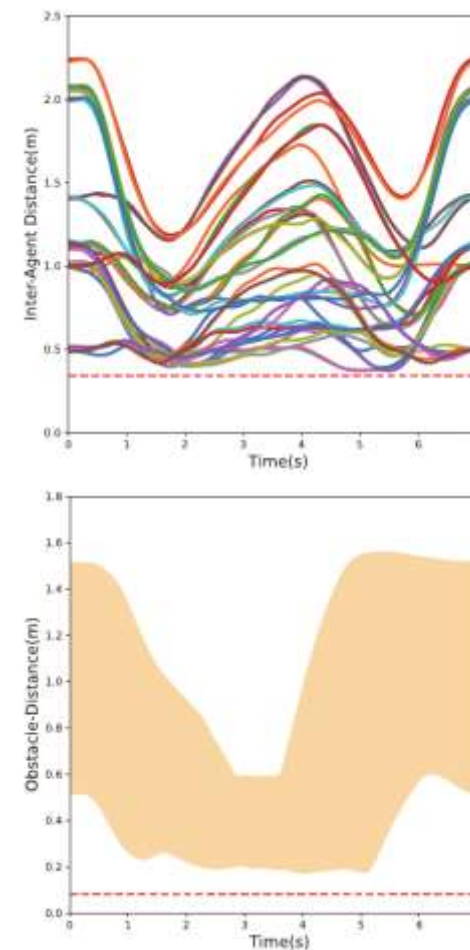
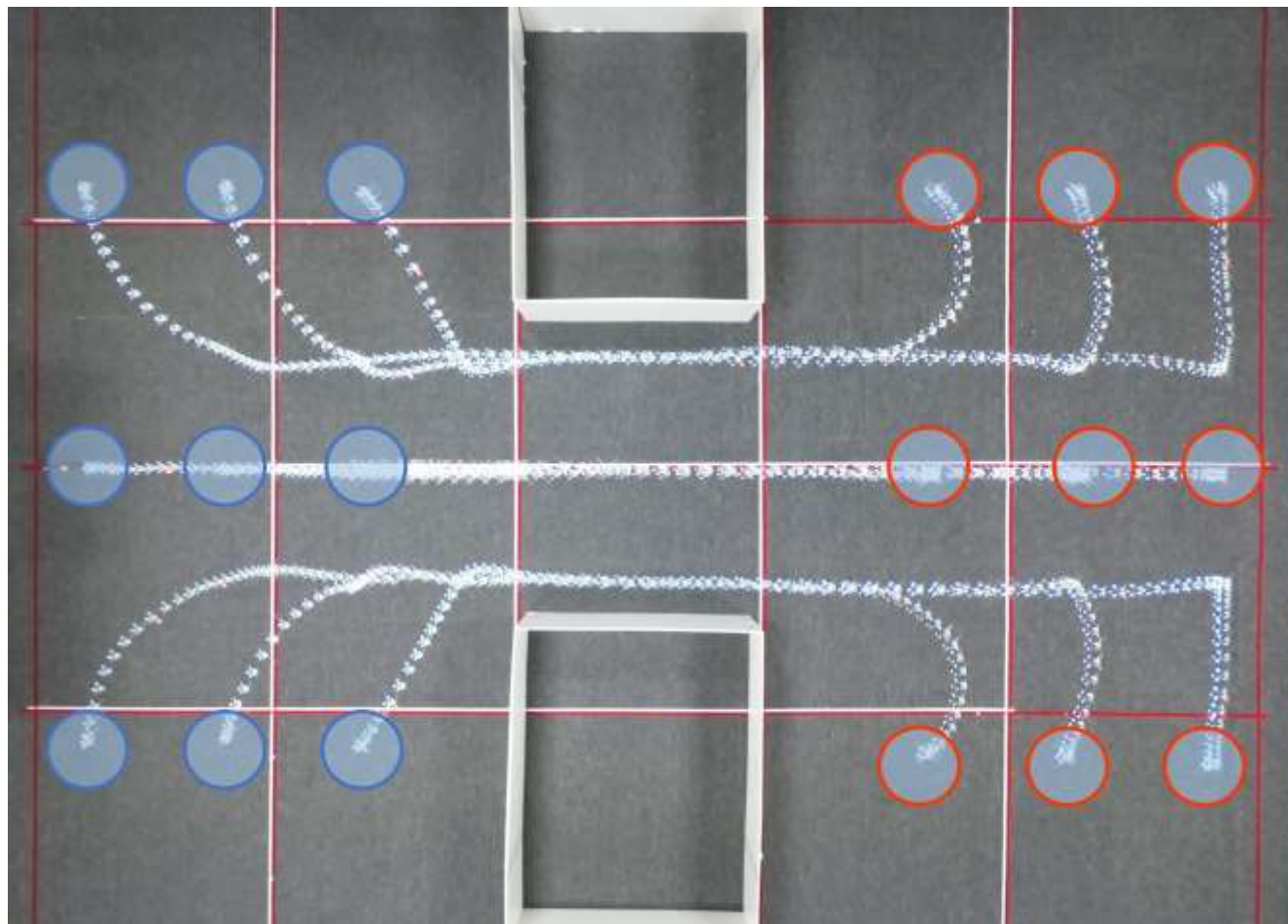


Left: The architecture of the hardware platform. Right: The testing ground.

Results



Experiment 1:

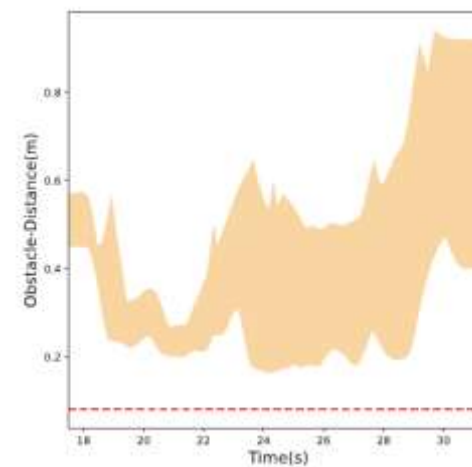
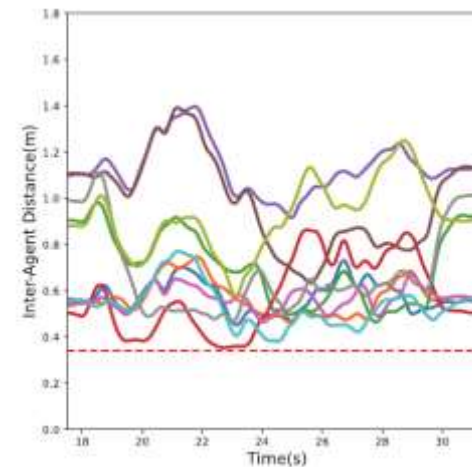
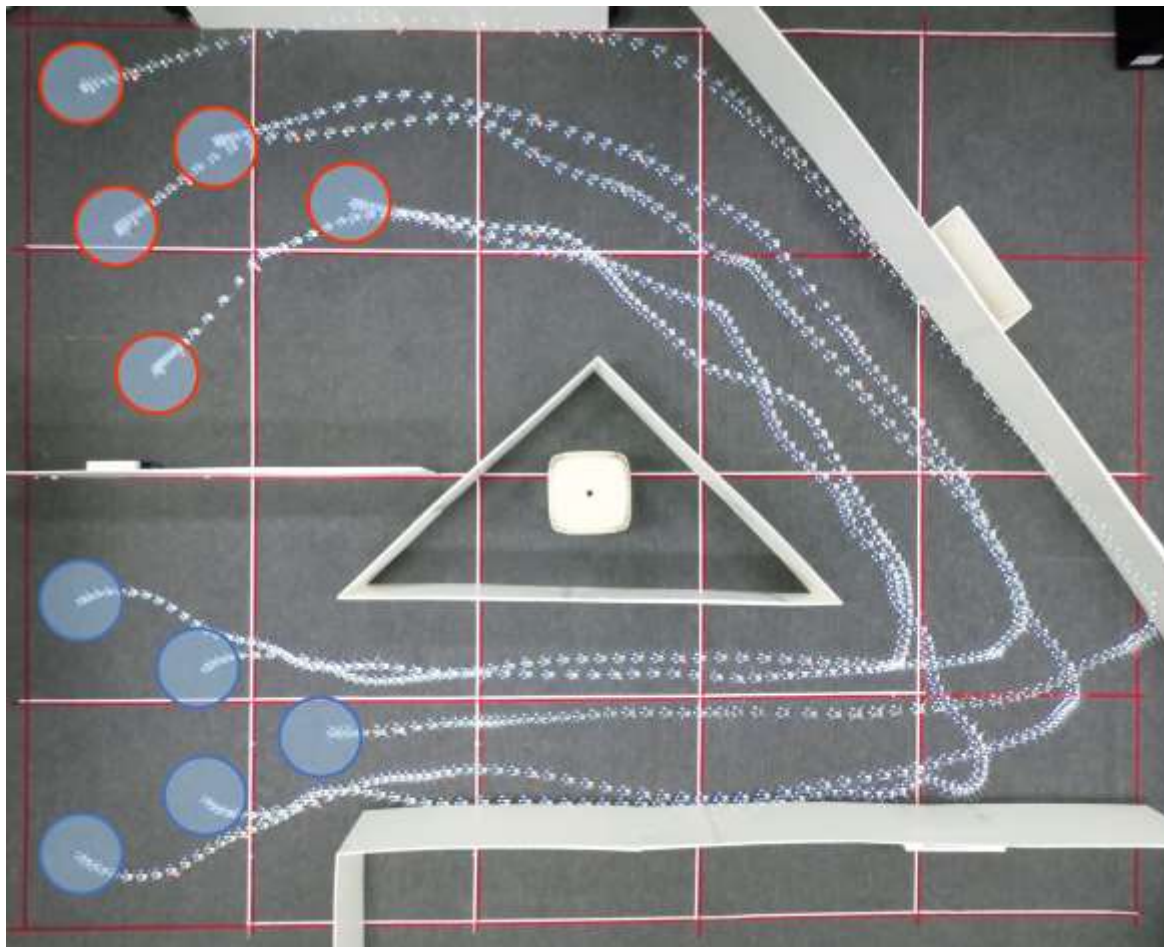


Left: The trajectories of agents. Right: The inter-agent and LOS-obstacles distance.

Results



Experiment 2:

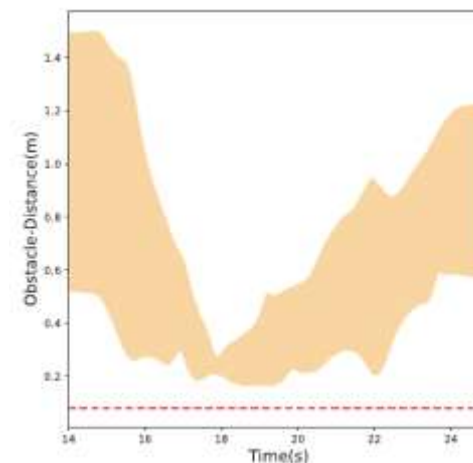
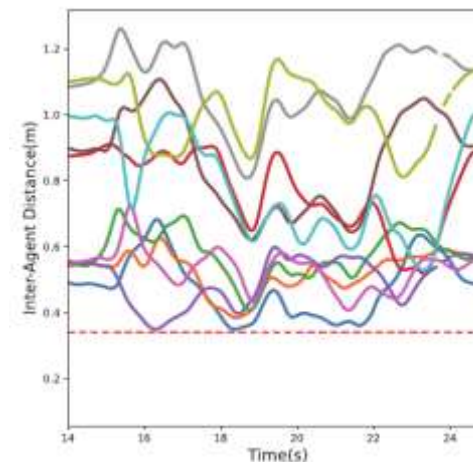
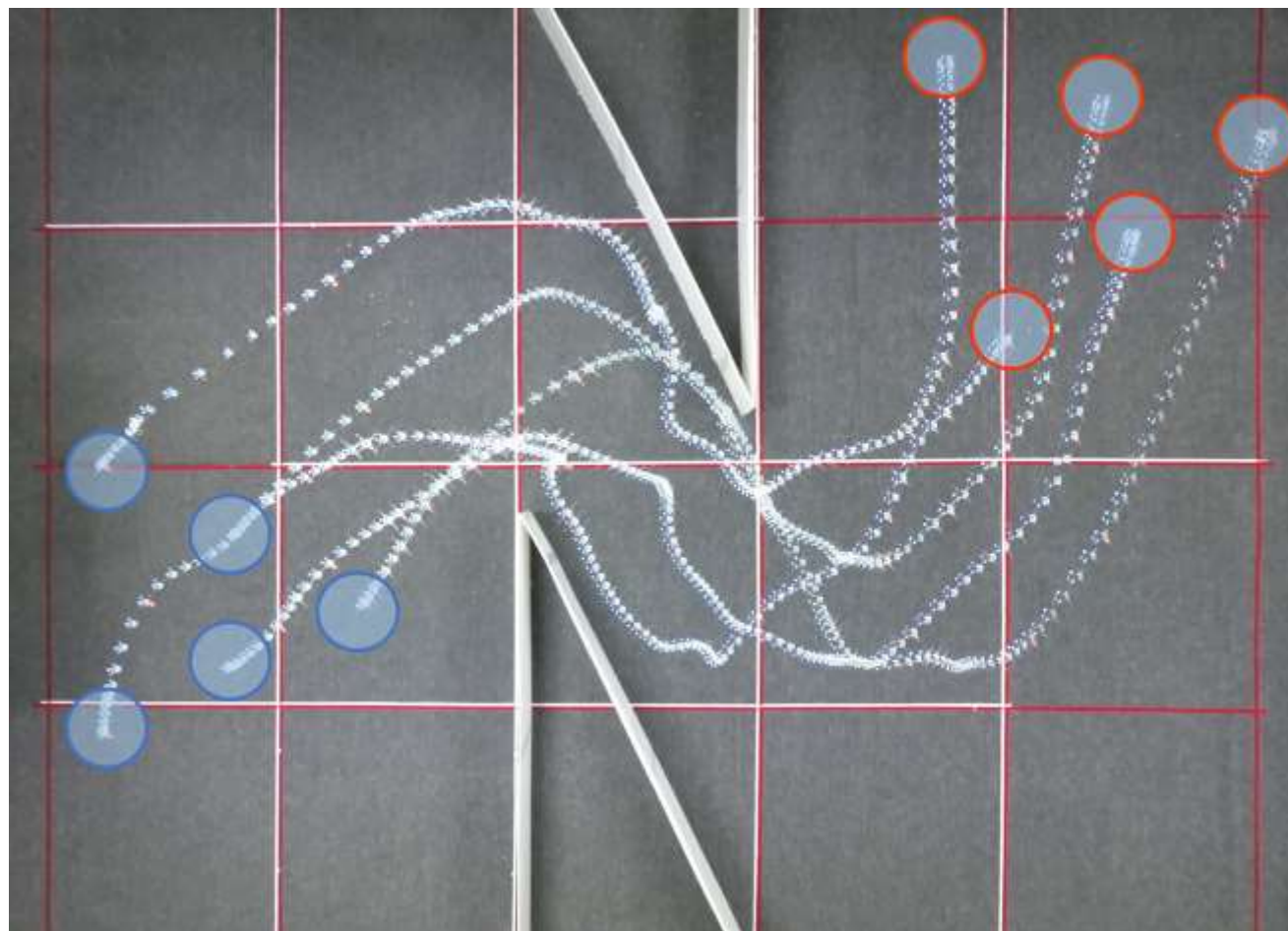


Left: The trajectories of agents. Right: The inter-agent and LOS-obstacles distance.

Results



Experiment 3:



Left: The trajectories of agents. Right: The inter-agent and LOS-obstacles distance.

- A formation adaptation method based on MPC-based trajectory planning, under which a swarms of agents can **flexibly adjust the formation structure** online to pass through narrow corridors and avoid obstacles
- Simulations and experiments are conducted to show the effectiveness and performance of the proposed scheme.
- Compared to previous related works, the advantages of the results in this paper are that the inter-agent connectivity can be maintained and the feasibility of the **underlying optimizations is guaranteed in a recursive way.**



Thank you!

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