

# DBKEM-AACS: a distributed key escrow model in blockchain with anonymous authentication and committee selection

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Dear editor,

Key security is of great practical significance and demand to guarantee the security of digital assets in the blockchain system. At present, users prefer to escrow their assets on centralized institutions, but this phenomenon has gone against the unique characteristics of decentralization and anonymity in the blockchain. Among them, the suspense incidents of assets lock or lost are enough to prove that the security of escrowed keys on the exchanges is questionable.

Based on the above problem, many scholars put forward the idea of combining threshold cryptography with key escrow. Moreover, the dynamic committee proactive secret sharing scheme (CHURP) [1] holds the function of updating periodical shares. However, there is still a lack of research on committee selection, anonymous authentication, and instantiation. The main contributions are as follows: (1) We propose an appropriate committee selection algorithm. (2) We propose an anonymous authentication scheme suitable for the blockchain system. (3) We construct a distributed key escrow scheme that can achieve anonymous authentication and committee selection.

*The proposed model.* The DBKEM-AACS is shown in Figure 1. Its main idea is as follows. Firstly, escrow node (EN) embedded physically unclonable functions (PUF) achieves the selection of key escrow committees, such as the old committee (OC) and the new committee (NC). Secondly, EN realizes identity authentication between EN and smart contract (SC). Finally, EN generates, distributes, verifies, and updates the key sub-shares, and then recovers the key. Some preliminaries are provided in Appendix A. The pseudocodes for all contracts are provided in Appendix B.

*Committee node selection algorithm.* Now, we design an appropriate committee node selection algorithm to deal with the lack of a committee selection method in CHURP [1] by referring to [2]. Especially, the randomness and positivity

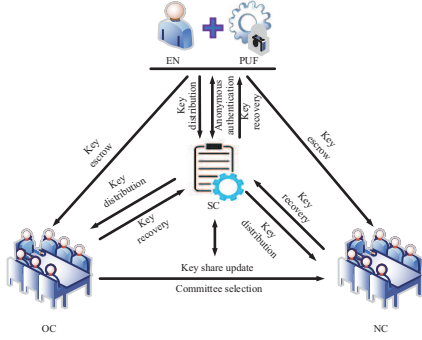
of nodes are guaranteed by the activeness and the honest behavior of nodes is restricted by deposits and rewards.

(1) Defining activeness. (a) Initializing. If the blockchain node (BN<sub>*i*</sub>) only participates in the transaction, the activeness calculation contract (ACC) computes an activeness  $A_i(e) = \min(0.5 + tx_i/tx, 1)$ . If (BN<sub>*i*</sub>) only participates in mining, ACC computes  $A_i(e) = \min(0.5 + wk_i/wk, 1)$ . If (BN<sub>*i*</sub>) do both, ACC computes  $A_i(e) = \min(0.5 + wk_i/wk + tx_i/tx, 1)$ . If BN<sub>*i*</sub> do not do either, ACC computes  $A_i(e) = 0.5$ . (b) Updating activeness. If BN<sub>*i*</sub> participates in the key escrow action during epoch *e*, then computes Eq. (1). If BN<sub>*i*</sub> does not participate in the key escrow action during epoch *e*, then computes Eq. (2).

$$A_i(e+1) = \begin{cases} \min\left(1, \left(1 + \frac{1}{e}\right) A_i(e)\right), & \text{if node submits correct key subshares;} \\ \max\left(0, \left(\frac{1}{1+e}\right) A_i(e)\right), & \text{if node does not submit key subshares;} \\ 0, & \text{if node submits incorrect key subshares.} \end{cases} \quad (1)$$

$$A_i(e+1) = \begin{cases} \min\left(1, A_i(e) + \left|\frac{wk_i}{wk}\right|\right), & \text{if node participates in mining;} \\ \min\left(1, A_i(e) + \left|\frac{tx_i}{tx}\right|\right), & \text{if node participates in transaction;} \\ \min\left(1, A_i(e) + \max\left(\left|\frac{wk_i}{wk}\right|, \left|\frac{tx_i}{tx}\right|\right)\right), & \text{if node participates in both mining and transaction;} \\ 0, & \text{if node submits incorrect key subshares.} \end{cases} \quad (2)$$

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**Figure 1** (Color online) The architecture of the DBKEM-AACS.

(2) Committee node selection contract (CNSC). (a) Initialization. EN inputs the deposit  $d_{en}$ , committee size  $N$ , public key  $pk_{en}$  and reward  $r$ , and each candidate node  $BN_i$  inputs  $A_i(e)$ ,  $pk_i$  and  $d_{BN_i}$  to CNSC. (b) Node sorting. After CNSC judges that its account balance is equal to  $d_{en} + n \times d_{BN_i}$ , it ranks  $BN_i$  according to  $A_i(e)$ , and storing the sorted result in the pre-committee node directory (PCND). (c) Committee selection. CNSC selects  $N$  nodes from PCND and inputs them into the committee node directory (CND), and then outputs the remaining nodes in PCND to the eliminated node directory (END) and returns their deposits or rewards.

*Anonymous authentication scheme based on PUF.* The purpose is to solve the problem of the key ownership by the node in the blockchain system. The designed node authentication contract (NAC): (a) Setup. Making some parametric assumptions that there is a secure channel, a constant  $k_i$ , and a hash function  $H$ . (b) Login.  $EN_i$  calculates  $d_i = H(N_i) \parallel pk_i \parallel (H(r_i) \oplus N_i)$  using PUF's return  $r_i$ , nonce  $N_i$  and  $H$ , and then inputs  $d_i$  to NAC. (c) Grant.  $EN_i$  calculates  $GM_i = d_i \parallel r_i \oplus m_i \parallel H(r_i \oplus m_i) \parallel \text{"Grant"} \parallel k_i$  after XORing a content  $m_i$  with  $r_i$ , and then inputs  $GM_i$  to NAC. (d) Authentication. After  $EN_i$  enters  $H(r_i)$  into NAC, it verifies  $k'_i \leq k$  and  $N_i$  in  $d_i$  by  $H(r_i)$ , searches and sends  $GM_i$  to  $EN_i$ , and then calculates  $k'_i = k'_i + 1$  and public on the blockchain. Finally,  $EN_i$  verifies the correctness of  $r_i \oplus m_i$  using  $H$ , and then obtains  $m_i$  by XORing  $r_i \oplus m_i$  with  $r_i$ . (e) Revocation. If  $k'_i > k_i$  is true, NAC publishes the message  $d_i \parallel r_i \oplus m_i \parallel \text{"Revoke"} \parallel k'_i$  on blockchain to revoke  $EN_i$ 's access permission to  $r_i \oplus m_i$ .

*Distributed key escrow scheme.* Now, we instantiate the theoretical idea of the "dimension-switching" [1] by specifying and disclosing one type of  $\langle t, 2t \rangle$ -order binary polynomial:  $B(x, y) = s + a_1x + a_2x^2 + \dots + a_tx^t + b_1y + b_2y^2 + \dots + b_{2t}y^{2t} + cxy$ . The execution items of the proposed key escrow contract (KEC) are as follows: (1) Initialization. calling CNSC to select OC:  $C_i^{(e)} = \{P_1^e, P_2^e, \dots, P_n^e\}$  and NC:  $C_i^{(e+1)} = \{P_1^{e+1}, P_2^{e+1}, \dots, P_n^{e+1}\}$ , calling NAC to complete the anonymous authentication of  $EN_i$  to the key sub-share  $B_i(h, y)$ . (a)  $B_i(h, y)$  generation.  $EN_i$  secretly constructs  $B_i(x, y) = sk_i + a_1^i x + a_2^i x^2 + \dots + a_t^i x^t + b_1^i y + b_2^i y^2 + \dots + b_{2t}^i y^{2t} + c^i xy$ .  $EN_i$  calculates  $B_i(h, y)$  for each node  $P_h^e$  in  $C_i^{(e)}$  and  $H(sk_i)$ , where  $h = 1, 2, \dots, n$ . (b)  $B_i(h, y)$  distribution. after  $EN_i$  securely inputs all  $B_i(h, y)$ ,  $H(sk_i)$  and  $pk_i$  into KEC, it calculates the secure sub-secret share  $c_h^i = B_i(h, y) \oplus r_h$  using  $P_h^e$ 's  $r_h$ ,  $s_h = c_h^i \parallel H(c_h^i) \parallel pk_h \parallel pk_i$  and publish  $s_h$  on the blockchain together with  $H(sk_i)$ . (c)  $B_i(h, y)$  verification.  $P_h^e$  retrieves  $s_h$  from the blockchain and verifies the correctness of  $s_h$  by using  $H$ ,  $c_h^i$ , and  $H(c_h^i)$ , and then obtains  $B_i(h, y)$  by calculating  $r_h \oplus c_h^i$ . (d)  $B_i(h, y)$

update (some details are provided in Appendix C). Firstly, KEC,  $P_h^e$ , each node in  $U' = \{C_i^{(e+1)}\}_{j \in \{2t+1\}}$  together construct  $B_i(x, j)$  to achieve share reduction [1] based on Eq. (3) and  $t+1$   $B_i(h_k, j)$ , where  $a_i, c(h_k), f(j)$  are all unknown. Secondly,  $U'_j$  calculates  $B'_i(x, j) = B_i(x, j) + Q_i(x, j)$  to achieve share proactvization [1] based on a 0-shared polynomial  $Q_i(x, j)$ .

$$\begin{cases} a_0 + a_1 h_1 + \dots + a_t (h_1)^t + f(j) + c(h_1)j = B_i(h_1, j), \\ a_0 + a_1 h_2 + \dots + a_t (h_2)^t + f(j) + c(h_2)j = B_i(h_2, j), \\ \vdots \\ a_0 + a_1 h_{t+1} + \dots + a_t (h_{t+1})^t + f(j) + c(h_{t+1})j \\ = B_i(h_{t+1}, j). \end{cases} \quad (3)$$

Finally,  $P_h^{e+1}$  in  $C_i^{(e+1)}$  constructs  $B'_i(h, y)$  to achieve full-share distribution [1] based on Eq. (4) and  $2t+1$   $B'_i(h, j_k)$ , where  $e_i, c(h)j_k, g(h)$  are all unknown.

$$\begin{cases} e_0 + g(h) + e_1 j_1 + \dots + e_{2t} (j_1)^{2t} + c(h)j_1 = B'_i(h, j_1), \\ e_0 + g(h) + e_1 j_2 + \dots + e_{2t} (j_2)^{2t} + c(h)j_2 = B'_i(h, j_2), \\ \vdots \\ e_0 + g(h) + e_1 j_{2t+1} + \dots + e_{2t} (j_{2t+1})^{2t} + c(h)j_{2t+1} \\ = B'_i(h, j_{2t+1}). \end{cases} \quad (4)$$

(e) Key recovery.  $EN_i$  constructs  $B'_i(x, y)$  based on Eq. (5) and  $t+1$   $P_h^{e+1}$ 's  $B'_i(h_k, y)$ , where  $sk_i, m_v, c(h_k), f(y)$  are all unknown but each  $f(y) + c(h_k)y$  is known, and  $t+1$  is the threshold value.

$$\begin{cases} sk_i + m_1 h_1 + \dots + m_t (h_1)^t + f(y) + c(h_1)y = B'_i(h_1, y), \\ sk_i + m_1 h_2 + \dots + m_t (h_2)^t + f(y) + c(h_2)y = B'_i(h_2, y), \\ \vdots \\ sk_i + m_1 h_{t+1} + \dots + m_t (h_{t+1})^t + f(y) + c(h_{t+1})y \\ = B'_i(h_{t+1}, y), \end{cases} \quad (5)$$

and then  $EN_i$  recovers  $sk_i = B'_i(0, 0) = B_i(0, 0)$ .

Security analysis and performance analysis are provided in Appendixes D and E, respectively.

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**Supporting information** Appendixes A–E. The supporting information is available online at [info.scichina.com](http://info.scichina.com) and [link.springer.com](http://link.springer.com). The supporting materials are published as submitted, without typesetting or editing. The responsibility for scientific accuracy and content remains entirely with the authors.

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