

### Supplementary:

**Proof of Theorem 1:** For the estimated error subsystem (11), we choose the Lyapunov function

$$V_e = e^T P^{-1} e, \quad (17)$$

where  $P = (p_{ij})(t)$  is a solution of the Riccati equation (10), then its derivative along the solution of (11) satisfies

$$\begin{aligned} \dot{V}_e &= e^T P^{-1} \dot{e} + e^T \dot{P}^{-1} e + e^T P^{-1} \dot{e} + e^T \dot{P}^{-1} e \\ &\leq -\frac{1}{2} e^T P^{-2} e + z_1^2 + 4h^2(t). \end{aligned} \quad (18)$$

Substituting  $\alpha_1 = -Kp_1^* p_2^* z_1$  in to (12), the  $z_1$  dynamics can be rewritten as

$$\dot{z}_1 = \left( -\frac{\dot{u}_0}{u_0} - Kp_1^* p_2^* \right) z_1 + e_2 + \sigma_1. \quad (19)$$

Selected a Lyapunov function candidate

$$V_1 = V_e + \frac{1}{2} z_1^2. \quad (20)$$

The derivative along the solution of (20) satisfies the following inequality

$$\begin{aligned} \dot{V}_1 &\leq -\frac{1}{2} e^T P^{-2} e + z_1^2 + \left( -\frac{\dot{u}_0}{u_0} - Kp_1^* p_2^* \right) z_1^2 \\ &\quad + z_1 e_2 + z_1 \sigma_1 + 4h^2(t) \\ &\leq \left( -\frac{1}{2} + \epsilon_1 \right) e^T P^{-2} e + \sigma_1^2 + 4h^2(t) \\ &\quad + \left( -\frac{\dot{u}_0}{u_0} - Kp_1^* p_2^* + 1 + \epsilon_2 \right) z_1^2, \end{aligned} \quad (21)$$

where  $\epsilon_1$  is a sufficiently small positive constant, while  $\epsilon_2$  is a suitable positive constant satisfying  $z_1 e_2 + z_1 \sigma_1 \leq \epsilon_1 e^T P^{-2} e + \epsilon_2 z_1^2 + \sigma_1^2$ . According to the second equation of the extended Kalman observer, i.e., equation (13), we have

$$\begin{aligned} \dot{\sigma}_1 &= \hat{z}_2 - \dot{\alpha}_1 \\ &= d_1(t) \hat{z}_3 - p_{21}(t) \hat{z}_2 + Kp_1^* p_2^* \dot{z}_1 + u \\ &= d_1(t) \hat{z}_3 - p_{21}(t) \hat{z}_2 - Kp_1^* p_2^* \frac{\dot{u}_0}{u_0} z_1 \\ &\quad - (Kp_1^* p_2^*)^2 z_1 + Kp_1^* p_2^* (e_2 + \sigma_1) + u. \end{aligned} \quad (22)$$

Therefore, the control law

$$u = -d_1(t) \hat{z}_3 + p_{21}(t) \hat{z}_2 + Kp_1^* p_2^* \frac{\dot{u}_0}{u_0} z_1$$

$$-L_1 \text{sgn}(\sigma_1) K |p_1^* p_2^* z_1| - L_2 \sigma_1, \quad (23)$$

with choice of the parameters as

$$\begin{aligned} L_1 &> Kp_1^* p_2^*, \quad Kp_1^* p_2^* \epsilon_2 \sigma_1 \leq \epsilon_3 e^T P^{-2} e + \epsilon_4 \sigma_1^2 \\ L_2 &> Kp_1^* p_2^* + \epsilon_4 + 2, \end{aligned} \quad (24)$$

for a sufficiently small  $\epsilon_3$  and a proper large  $\epsilon_4$ , renders

$$\sigma_1 \dot{\sigma}_1 \leq \epsilon_3 e^T P^{-2} e - 2\sigma_1^2. \quad (25)$$

Consider the Lyapunov function candidate

$$V_2 = V_e + \frac{1}{2} z_1^2 + \frac{1}{2} \sigma_1^2. \quad (26)$$

From (22) and (26), we obtain the time derivative of  $V_2$  satisfies

$$\begin{aligned} \dot{V}_2 &\leq \left( -\frac{1}{2} + \epsilon_1 + \epsilon_3 \right) e^T P^{-2} e - \sigma_1^2 + 4h^2(t) \\ &\quad + \left( -\frac{\dot{u}_0}{u_0} - Kp_1^* p_2^* + 1 + \epsilon_2 \right) z_1^2. \end{aligned} \quad (27)$$

Since the adjustable parameters  $K, L_1, L_2$  and  $\epsilon_i, i = 1, 2, 3, 4$ , can be set as required, while  $\dot{u}_0/u_0$  is bounded, therefore, if

$$-\frac{\dot{u}_0}{u_0} - Kp_1^* p_2^* + 1 + \epsilon_2 < 0, \quad -\frac{1}{2} + \epsilon_1 + \epsilon_3 < 0,$$

is guaranteed, then the inequality (27) yields

$$\dot{V}_2 \leq -\beta V_2 + 4h^2(t), \quad \beta > 0. \quad (28)$$

Noting that  $h(t) \in l_2$ , it can be proved that  $V_2$  converges to zero asymptotically, which implies that the signals  $e, z_1$  and  $\sigma_1$  verge to zero as time tends to infinity. By the definitions of  $e_i = z_i - \hat{z}_i$  ( $i = 1, 2, 3$ ),  $\sigma_1 = \hat{z}_2 - \alpha_1$  and the fact that  $\alpha_1 = -Kp_1^* p_2^* z_1$ , it is derived that  $\hat{z}_2$  and  $z_2$  go to zero. Moreover, noting that  $\dot{z}_3 = h(t)$  and  $h(t) \in l_2$ , it is concluded that  $z_3$  as well as  $\hat{z}_3$  is bounded. Therefore, the control law given in (23) is bounded, and moreover, as time tends to infinity,  $u + d_1 \hat{z}_3$  tends to zero. As a result, from the inverse transformations of coordinate/state, we can obtain that  $x_1, x_2$  converge to zero. This together with the design of (2) indicates that  $(x_1, y_l, \theta_l)$  converges to the equilibrium  $(0, 0, -\epsilon)$ .